## 2014-2015 Primary Solutions Round I

## P1.1

Chris has found a three-digit number. The number which uses some of the figures $0, I, \ldots, 9$ can be read back to front and upside down but it stays the same.

Find all the possibilities for Chris's number.

## Solution

IOI, III, I8I, 808, 818, 888

## P1.2

How many whole numbers between 1 and 1000 do not contain the digit 1 ?

## Solution

A reasonable strategy is count the numbers which contain 1.
Between 1 and 99 , numbers 1,10 to 19 , and $21,31, \ldots 91$ contain 1 (at least once), i.e. 19 numbers.
Numbers from 100-199 all contain the digit 1 i.e. 100 in total.
Between 200 and 299 a further 19 numbers contain the digit 1, and similarly for each further hundred, i.e. $8 \times 19$ in all.
Finally, 1000 contains the digit 1.
Overall $9 \times 19+100+1=272$ contain the digit 1 , and so $1000-272=728$ do not contain the digit 1.

## P1.3



Three different ways of dividing a $3 \times 3$ square into one $1 \times 1$ square and four $2 \times 1$ rectangles are shown above. How many ways are there in all (including the ones shown above)?

## Solution

The second diagram is a rotation of the first, and the third is a mirror image of the first. So we must count mirror images and rotations separately.

There are 4 ways with the $1 \times 1$ square in the top left corner:

and hence $4 \times 4=16$ ways with a $1 \times 1$ square in any corner.
It is not possible to cover the $3 \times 3$ square when the $1 \times 1$ square is in the centre of an edge.
There are 2 ways with the $1 \times 1$ square in the centre, which are mirror images:


This gives a total of 18 ways.

